DYNAMIC PRICING FOR AIRLINE ANCILLARIES WITH CUSTOMER CONTEXT

BY

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THESIS

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ABSTRACT

Ancillaries in the travel industry have become a major source of income and profitability. However, conventional pricing strategies are based on poorly optimized business rules that do not respond to changing market conditions.

This study describes the dynamic pricing model that we have developed in conjunction with Deepair solutions, an AI technology provider for travel suppliers. We present a pricing model that provides dynamic pricing recommendations specific to each customer interaction and optimizes expected revenue per customer. The unique nature of personalized pricing provides the opportunity to search over the market space to find the optimal price-point of each ancillary for each customer, without violating customer privacy.

In this study, we present and compare three approaches for dynamic pricing of ancillaries, with increasing levels of sophistication: (1) a two-stage forecasting and optimization model using a logistic mapping function; (2) a two-stage model that uses a deep neural network for forecasting, coupled with a revenue maximization technique using discrete exhaustive search; (3) a single-stage end-to-end deep neural network that recommends the optimal price. We describe the performance of these models based on both offline and online evaluations. We also measure the real-world business impact of these approaches by deploying them in an A/B test on an airline’s internet booking website. We show that traditional machine learning techniques outperform human rule-based approaches in an online setting by improving conversion by 36% and revenue per offer by 10%. We also provide results for our offline experiments which show that deep learning algorithms outperform traditional machine learning techniques for this problem.

Additionally, we propose a meta-learning approach for synchronous deployment of multiple models. This approach is currently under production with our partner airline. Our end-to-end deep learning model is currently being deployed by the airline in their booking system.
To my parents, for their love and support.
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CHAPTER 1: INTRODUCTION

1.1 BACKGROUND

Ancillaries are optional products or services sold by businesses to complement their primary product [1]. In the airline industry, these services or products can be directly related to a passenger’s flight itinerary, such as baggage allowance, leg room, seat upgrades or meals, or may be related to the passenger’s overall travel plan, for example, hotel rooms, rental cars, or destination activities. The estimated ancillary revenue collected by major US air carriers was more than $18 billion in 2015, and $59 billion for airlines around the world in the same year [2].

Even though this revenue stream is clearly substantial to the airline industry, its pricing strategies are not fully developed due to its recent emergence in the market. Because these products were traditionally not offered as ancillaries, airlines have little knowledge of the relationship between the customers’ choice of primary product and the ancillary product. Moreover, given the now optional nature of these products, ancillary purchases are a result of deep personal preferences of each individual and the context of their trip. Consequently, airlines experience very low conversion rates (less than 5%) for ancillaries. Understanding these personal preferences based on the context of each shopping session is crucial to pricing them effectively and generating revenue. Moreover, various ancillaries compete with each other’s ”shelf-space” on the website and wallet-share of the customer, so pricing an ancillary in the context of other ancillaries confounds the problem.

Currently, the majority of ancillary products are static price-points, i.e., invariant to customer or itinerary characteristics. Our aim is to develop a price recommendation system specific to ancillary services, to price these products dynamically based on itinerary-specific information.

Each booking session on an airline’s website can be modeled using the state space represented in Figure 1.1. The first three steps involve the primary product, which is a set of seats on aircraft connecting the origin to the destination, referred to as right-to-fly; while ancillary offerings and corresponding customer choice occur from state 4 onwards. Note that in this work we consider only ancillaries offered during the booking session, and not those booked later, such as adding bags after reaching the airport. The goal of this work is to optimize prices dynamically, while estimating willingness to pay; and therefore we will address the latter case in future work.

Conventional pricing frameworks are static, and not capable of recommending a price
conditioned upon rich session-specific information. Our pricing suggestions are generated through an A/B testing framework that directs live booking traffic to various deployed models. The integration specifications for inference and data retrieval for training, with respect to the current pipeline at an airline booking engine, are described in Figure 1.2.

Our contributions are as follows.

• We present a rich, customized, session-specific dynamic price recommendation system for ancillary services that significantly outperforms existing pricing systems in terms of revenue.

• We develop a deep learning model that effectively estimates purchase probability and simultaneously prices the ancillary product, by modeling monotonicity properties of customers’ willingness to pay. This model provides improved revenues and captures customers’ behavior more accurately than sequential models that combine traditional machine learning (or deep learning) models followed by revenue optimization.

• Our model predicts human choice more accurately than our baseline model, resulting in increased conversion for the ancillary product.

• We implement and test our models on real data, both on historical data and by live
testing in an airline’s booking system, and demonstrate both offline and online improvement based on live customer usage statistics.

1.2 RELATED WORK

Unbundling is the process of separating a product into primary and ancillary products to allow customers more flexibility of purchase, and businesses to increase revenues by matching customer needs more accurately. In the airline industry, this phenomenon has been led by low-cost carriers (LCCs), whose operational and pricing models rely heavily on ancillary fees. In recent years, many legacy airlines have adopted this strategy [3]. Despite an initial response through negative emotions and retaliatory behavior [4], unbundling of services into the basic right-to-fly and additionally priced ancillary services (bags, meals, etc.) has gradually gained acceptance among customers [5]. In fact, revenue from ancillary services in
the airline industry have nearly tripled in the past decade, from 3% to 8% of total revenue [6].

Studies on this new phenomena in the airline context are ongoing [7, 8]. Economics literature indicates that the practice of offering add-ons (an equivalent term for ancillaries) can raise equilibrium profits when airlines compete; and can also be used for price discrimination and customer segmentation [9]. Allon et al [8] argue that unbundling and baggage fees are consistent with reduction of airline operating costs, but may not effectively segment customers. Customer characteristics and the airline’s ability to price discriminate are also shown to significantly influence its profits [7]. Bockelie and Belobaba [1] study behavioral models of ancillary product purchase, and specifically comparing the difference in price perceptions of customers who purchase ancillary services sequentially or simultaneously. While multiple behavioral theoretical models [10, 11, 12] based on risk perception, knowledge levels and bounded rationality; and discrete choice models [13] are typically used to model customer choice, there is limited literature that explicitly models the relationship between ancillary services and the primary product (itinerary, or fare class).

Carrier et al [14] discussed passenger choice models extensively and extended booking-based passenger choice models to the joint choice of an airline itinerary and fare product. Also, additional studies provide analytical insights on the dependence of pricing models on factors involving flow of the LCC’s like infrastructural, institutional and geographic factors [15]. This suggests a far deeper dependence of offered service’s price on factors involving customers and airline. Additionally, it has been studied that strategic implementation of ancillaries in a market of heterogeneous customers requires a fine understanding of price sensitivity. Customers sensitivity and specificity in service policies help providers to deliver services at lower prices to majority of the customers while sustaining the revenue margins [16, 17]. Hence, the opportunity to model customer’s behaviour lies in correctly estimating market’s sensitivity and demand based on customers context which inherently depends on the factors mentioned above.

Deep neural networks have shown tremendous success on context based modeling in the field of computer vision [18, 19, 20], natural language processing [21, 22], reinforcement learning [23, 24, 25] and others [26] as well. Also, Hornik et al [27] prominently established that the multilayer feed forward network are the universal approximators. In addition to that, deep neural networks have been successful in modeling highly non-linear systems including fuzzy models [28]. Hence, this approach is an effective way of capturing extremely non-linear dependencies in customers’ context to map market’s demand and sensitivity. Uber [29], Lyft [30] and Airbnb [31] have effective dynamic pricing based on customers context using recent machine learning advancements. Moreover, many other industries like electricity markets
[32], stock markets [33] and energy markets [34] that were traditionally using static analytic based approaches to price their products are now dynamically pricing based on recent machine learning and deep learning models.

Topics in dynamic pricing of homogeneous products have been extensively studied [35]. In fact, dynamic pricing has been a catalyst for innovation in various transport and service industries. Ride-hailing platforms have used surge pricing to match demand and supply, and to avoid the “wild-goose chase” problem [29]. Related to our problem is the work of P. Yu and J. Qian [31] for Airbnb accommodation pricing. They formulate a custom scheme to optimally price each product using a triple-stage model with booking probability classification, price-suggestion regression and seller-specific logic. Whereas Airbnb considers all their listings as unique and all the customers identical, we consider the inverse problem of identical products and unique customers.
CHAPTER 2: PRICING FACTORS

To correctly estimate the demand of the customers based on their specific context, analysis of the factor of dependence is necessary. The static prices for such ancillaries are traditionally decided based on some of these factors of dependence. Analysts use the pricing factors to decide the suitable price for the offered ancillary. Hence, it is crucial to investigate the pricing factors to price the ancillary correctly. In this chapter, we discuss the two primary factors we use to determine the optimal price for an ancillary: the demand function and customer attributes.

2.1 DEMAND FUNCTION

An estimation of a demand curve $D(P)$ as a function of price $P$, can be obtained by evaluating the variation of demand with respect to price. Then, the optimal price can be obtained via maximizing the expected revenue based on the estimated demand curve. The optimal value can only be obtained when the demand function $D(P)$ is an accurate estimate of the actual demand in the market, else the $P^*$ and corresponding revenue will be sub-optimal.

$$P^* = \arg\max_P P \times D(P)$$ (2.1)

For airline ancillaries, the demand function $D$ is not just a function of price $P$ offered but also of customer attributes $\mathbf{x}$. Hence, a better estimation of the demand function is $D(P, \mathbf{x})$ and can be obtained by observing the change in demand conditioned on both price $P$ and customer attributes $\mathbf{x}$. In our study, we implement and compare two algorithms to estimate the probability of a customer purchasing an offered ancillary, which we assume to be a proxy for estimated demand $D(P, \mathbf{x})$. Details of our algorithms are presented in Chapter 3.

2.2 CUSTOMER ATTRIBUTES

We define a customer’s attributes, $\mathbf{x}$, as the set of factors that influences the probability of that customer purchasing the offered ancillary, at a given price. The major attributes that the demand function is found to be significantly dependent on are time, market, items already in the cart and length of stay.
2.2.1 Time

There are two types of time-related factors that heavily influence the demand function: (1) Days to departure: Price sensitivity captures the relationship between the price and the propensity for purchasing the product. Usually, customers who buy their tickets far in advance are more price sensitive than customers who buy closer to departure. (2) Departure date and time: Like the right-to-fly, ancillary demand has strong time-of-day and seasonal variations. Itineraries starting on certain days and times have higher ‘quality’ and hence increased demand; due to factors such as higher convenience of time of travel, better connectivity (neither too long nor too short connection time), better availability of alternative connections, special events, and holidays. The quality of service has a strong correlation with the type of passengers it attracts. It is well-known that low quality services tend to be cheaper and attract more price sensitive customers.
2.2.2 Markets

Airlines serve a large variety of markets. A market is a tuple comprising of the origin and destination of the trip. Certain markets are served with a larger fraction of non-stop itineraries, while others may be served with larger fractions of itineraries containing connections. Certain markets have a heavier fraction of business trips, while others consist primarily of leisure trips.

As shown in Figure 2.1, there are clusters of markets that have high demand for ancillary services as compared to others. To estimate the demand using (2.1), we segment these clusters into sub-markets. We define sub-markets as a mapping from a vector of customer attributes $\mathbf{x}$ to an origin-destination cluster where estimated demand is statistically similar for a given prior ancillary price.

Visualization of historical purchases with t-SNE produces apparent separation with about 15 discrete clusters as shown in Figure 2.2. The colours are destination airports, which do not associate with the formed clusters. Also, note that the axis represented in Figure 2.2 are the primary principal components. This signifies the presence of latent variable which determines the basis of cluster formation. Similarly, the t-SNE plot of instances where the ancillary is purchased (orange) and not purchased (blue) is shown in Figure 2.3. This indicates the presence of clusters where probability of purchase is significantly higher than
others. Also, some “all-blue” (no purchase) clusters are present.

Segmenting clusters of markets based on the historical demand for ancillaries seems an important factor in estimating the demand function defined in equation (2.1).

2.2.3 Length of Stay

For those passenger bookings that are round-trips, we define Length of stay (LOS) as the number of days a passenger plans to stay at the destination. If the passenger does not have a return ticket we consider LOS to be 0. Figure 2.4 shows the estimated kernel density function for LOS for two types of bookings: when an ancillary was purchased (dashed line), and for all bookings (solid line). These estimated graphs are irregular from normalized LOS values of 0.0 to 0.3 (approximately), indicating higher chances of ancillary purchase for LOS durations that are neither too short nor too long. These irregularities indicate that passengers prefer to purchase ancillaries (such as bags), for medium length trips for which they might require additional storage space. Hence, the apparent signature describes the conditional importance of the LOS attribute.
Figure 2.4: LOS signal from KDE
In this chapter, we discuss the models used to price the ancillary given the customer context. Our pricing model consists of two components: (i) an ancillary purchase probability model that is structured as a binary classification problem, and (ii) a revenue optimization model that, given the probability of purchase, recommends an optimal price that maximizes the airline’s expected revenue.

We make the following assumptions:

- **Pricing range**: The recommended ancillary price is allowed to vary only within a legal range defined by business strategy as mentioned in Section 4.4.

- **Monotonicity in willingness to pay**: If a customer is willing to purchase a product for price $p$, they are willing to purchase the same product at a price $p' < p$. Similarly, if a customer is unwilling to purchase a product at price $p$, they will be unwilling to purchase at a price $p' > p$.

We implement three different pricing models, of increasing complexity, shown in Figure 3.1. These are embedded into the framework in Figure 1.2.

1. **Ancillary purchase prediction with logistic mapping (APP-LM)**: This model uses a Gaussian Naive Bayes with clustered features (GNBC) model for ancillary purchase probability prediction and a pre-calibrated logistic price mapping function for revenue optimization.

2. **Ancillary purchase prediction with exhaustive search (APP-DES)**: This model uses a Deep-Neural Network (DNN) trained using a weighted cross-entropy loss function for ancillary purchase probability estimation. For price optimization, we implement a simple discrete exhaustive search algorithm that finds the optimal price point within the pricing range.

3. **End-to-End DNN with custom loss function (DNN-CL)**: This DNN-based model is trained on a customized loss function, and presented in Section 3.3. This loss function is designed using the strategic model objective function[31] and explicitly models the dominance properties embedded within the willingness to pay assumption.

In APP-LM and APP-DES, the ancillary purchase probability model and the revenue optimization model are sequential whereas in DNN-CL, they are simultaneously solved to achieve the recommended price.
3.1 ANCILLARY PURCHASE PROBABILITY MODEL

Our ancillary purchase probability model estimates the demand curve within a sub-market for each offered ancillary, for a given price of the ancillary. This is formulated as a binary classification problem. We aim to estimate the probability distribution function $f_\theta(x, P)$, where $x | x \subseteq x$, is the feature vector and $P$ is the offered price. We used over 30 features that fall under the following categories:

- **Temporal features**: Length of stay, seasonality (time of the day, month of the year, etc), time of departure, time of shop, time to departure.

- **Market-specific features**: Arrival and destination airport, arrival and destination city, ancillary popularity for the route, etc.

- **Price comparison scores**: Scores based on alternative/same flights across/within the booking class.

- **Journey specific features**: Group size, booking class, fare group, number of stops, etc.

As mentioned earlier, the binary classification task is highly challenging because ancillary purchase is highly imbalanced (class ratios of $6:100$). For APP-LM, We first experiment with many traditional classification algorithms like Gaussian Naive Bayes (GNB), Gaussian Naive Bayes with clustered features (GNBC), Random Forest (RF), using features chosen based on principal component analysis for these algorithms [36].

For APP-DES, we use a customized deep neural network (DNN) trained on weighted cross entropy loss, as a classifier. While the DNN did not require a lot of feature engineering, we experimented with various hyper-parameters like network architecture, drop-out rates, activation functions, optimization algorithms, and convergence criteria.
3.2 REVENUE OPTIMIZATION

Revenue optimization is standard technique used by analysts to decide the price of a product based on historical data. Here the idea is to maximize the expected revenue based on demand function which is conditioned upon offered price.

3.2.1 Logistic Price Mapping Function

In our base model APP-LM, once the ancillary purchase probability is predicted, we use a logistic function to recommend a price. The intuition behind using logistic mapping is that the ancillary can be priced closer to the maximum of the pricing range when the probability of purchase is high, and lower for low probabilities. Hence, a price mapping is chosen based on (3.1).

\[ P_{\text{rec}} = \frac{L}{1 + \exp^{-k(x-x_0)}} \]  

Figure 3.2: Logistic mapping from probability of purchase to a recommended price.

According to (3.1), three parameters can be controlled to map the price desirably.

- Max value, \( L \) : this is the full price of the ancillary
- Shape factor, \( k \) : the shape or steepness of the curve
- Mid point, \( x_0 \) : the mid point of the sigmoid curve
The shape factor $k$ and mid-point $x_0$ can be fine-tuned to be either aggressive or conservative with pricing. This tuning is illustrated in Figure 3.2, indicating that at low purchase probabilities, the model compensates by reducing the recommended price.

\begin{algorithm}
\caption{APP-LM Inference}
\begin{algorithmic}[1]
\For {$t = 1, 2, \ldots$}
\State $x_t \leftarrow \text{Preprocessing}(x)$
\State $\hat{P} = P_{\text{standard}}$
\State Predict the probability $p \leftarrow f_\theta(x_t, \hat{P})$
\State Recommend the price $P_{\text{rec}} = \frac{L}{1 + \exp^{-k(p-x_0)}}$
\State Observe and record ground truth $y_t \leftarrow \text{Offer}(P_{\text{rec}})$
\EndFor
\end{algorithmic}
\end{algorithm}

3.2.2 Discrete Exhaustive Search

Exhaustive search can be efficiently performed over a small set of discrete prices that are within the pricing range. For a given probability of purchase $f_\theta(x, P)$ and price $P$, expected revenue is computed using (3.2).

![Figure 3.3: An illustration of a discrete search in the price range](image-url)
\[ \hat{E}_P = P \times f_\theta(x, P) \] (3.2)

Without assuming that the revenue function is convex but only unimodal, an exhaustive search over all allowed prices can be performed, as represented in Figure 3.3. The convexity assumption is met only when price sensitivity has a small derivative in the region of interest. Thereby, using exhaustive search, the optimal price can be evaluated using equation 3.3. As discussed in Section 2.1, the optimality of the price \( P^{ree} \) is dependent on the accuracy of estimation of the demand.

\[ P^{ree} = \arg\max_P \hat{E}_P \] (3.3)

Algorithm 2 APP-DES Inference

1: for \( t = 1, 2, \ldots \) do
2: \( x_t \leftarrow \text{Preprocessing}(x) \)
3: for \( \hat{P} = P_1, \ldots, P \) do
4: \( p \leftarrow f_\theta(x, \hat{P}) \)
5: \( \hat{E}_\hat{P} = \hat{P} \times p \)
6: end for
7: Recommend ancillary price
8: \( P^{ree} = \arg\max_P \hat{E}_P \)
9: Observe and record ground truth
10: \( y_t \leftarrow \text{Offer}(P^{ree}) \)
11: end for

The performance of a two-stage sequential forecasting and optimization method (like APP-LM and APP-DES), depends on a good demand estimate over the permissible range of prices. This requires sufficient exposure of those prices in the market to learn an accurate price sensitivity curve for each sub-market. Without such data, approximate methods such as custom loss functions can produce more revenue in practice.

3.3 CUSTOMIZED LOSS FUNCTION FOR DNN-CL

In this section, we present a customized loss function that takes into account a regret of pricing low, conditional on the ancillary being purchased; and a penalty for recommending
high, conditional on it not being purchased. The objective function is inspired from the strategic model proposed by [31] and \( \epsilon \)-insensitive loss used in SVR[37]. We enhance this strategic model using latent variables to incorporate the monotonicity in the willingness to pay assumption in our loss function. Suppose we are given \( N \) training samples \( \{x_i, y_i\}_{i=1}^{N} \), where \( x_i \) is the feature vector and \( y_i \) is the ground truth label for the \( i^{th} \) session. For purchased ancillaries, \( y_i \) equals 1 and 0 otherwise. The recommended price \( P_{rec} \) for feature vector \( x \) is denoted by \( P_{rec} = \mathbb{F}_\Theta(x, \mathbb{P}) \), where \( \Theta \) is a set of trainable parameters that can be learned for the mapping function \( \mathbb{F} \), and \( \mathbb{P} \) is a set of discrete price points in the pricing range.

The objective of the learning is to minimize the loss \( \mathcal{L} \) given as

\[
\mathcal{L} = \arg\min_{\theta} \sum_{i=1}^{N} \sum_{j=1}^{|\mathbb{P}|} (\Phi_{lb} + \Phi_{ub}) \cdot \mathbb{1}_{(\sigma_{ij} > 0)} \tag{3.4}
\]

where the lower bound function \( \Phi_{lb} \) and upper bound function \( \Phi_{ub} \) are defined as,

\[
\Phi_{lb} = \max \left( 0, \left( L(P_{ij}, \delta_{ij}) - \mathbb{F}_\Theta(x_i, \mathbb{P}) \right) \right)
\]

\[
\Phi_{ub} = \max \left( 0, \left( \mathbb{F}_\Theta(x_i, \mathbb{P}) - U(P_{ij}, \delta_{ij}) \right) \right)
\]

where \( \delta_{ij} \), shown in Figure 3.4, is a latent variable that ensures the monotonicity in the willingness to pay assumption by taking the current ground truth \( y_i \) into account. The indicator function \( \mathbb{1}_{(\sigma_{ij} > 0)} \) selects loss values corresponding to those \( \delta_{ij} \) which satisfy the monotonicity condition. Therefore, \( \delta_{ij} \) is defined as

\[
\delta_{ij}(y_i) = \begin{cases} y_i & \text{if } \sigma_{ij} \geq 0 \\ 0 & \text{otherwise} \end{cases} \tag{3.5}
\]

Where, \( \sigma \) is the willingness to pay factor, defined as:

\[
\sigma_{ij} = (j - j^*) \cdot (-1)^{y_i} \tag{3.6}
\]

Assuming prices are listed in ascending order, \( j^* \) is the index at which \( P_{ij} \) equals \( \mathbb{F}_\Theta(x_i, \mathbb{P}) \). We use \( L \) and \( U \) for the lower bound and the upper bound of the optimal price range, respectively. The functions \( L(P_{ij}, \delta_{ij}) \) and \( U(P_{ij}, \delta_{ij}) \) are defined as follows:

\[
L(P_{ij}, \delta_{ij}) = \delta_{ij} \cdot P_{ij} + (1 - \delta_{ij}) \cdot c_1 P_{ij} \tag{3.7}
\]
Figure 3.4: Latent variable $\delta$ mapping from ground truth $y$

When the ancillary is purchased, the lower bound $L$ is the purchase price $P_{ij}$. Otherwise, a lower price of $c_1 P_{ij}$ is set to be the lower bound, where $c_1 \in (0, 1)$.

$$U(P_{ij}, \delta_{ij}) = (1 - \delta_{ij}) \cdot P_{ij} + \delta_{ij} \cdot c_2 P_{ij}$$  \hspace{1cm} (3.8)

The upper bound $U$ is $P_{ij}$ when the ancillary is not purchased, whereas if the ancillary is purchased, a price of $c_2 P_{ij}$ ($c_2 > 1$) is set as the upper bound.

Table 3.1: Lower bound and Upper bound loss values

<table>
<thead>
<tr>
<th>Prices</th>
<th>$\Phi_{lb} \cdot \mathbb{I}(\sigma_{ij} &gt; 0)$</th>
<th>$\Phi_{ub} \cdot \mathbb{I}(\sigma_{ij} &gt; 0)$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$P_{ij} &lt; F_{\Theta}$</td>
<td>0</td>
<td>$\max(0, F_{\Theta}(x_i, \mathbb{P}) - c_2 P_{ij})$</td>
</tr>
<tr>
<td>$P_{ij} = F_{\Theta}$</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>$P_{ij} &gt; F_{\Theta}$</td>
<td>$\max(0, c_1 P_{ij} - F_{\Theta}(x_i, \mathbb{P}))$</td>
<td>0</td>
</tr>
</tbody>
</table>

Table 3.1 illustrates the lower and upper bound loss values for recommended price with respect to discrete price points. For $P_{ij} < F_{\Theta}(x_i, \mathbb{P})$, the upper bound loss increases linearly. For upper bound loss to be non-zero, $c_2 > \frac{F_{\Theta}(x_i, \mathbb{P})}{P_{ij}}$. Similarly, for non-zero loss, the bounds on $c_1$ are set to $\frac{F_{\Theta}(x_i, \mathbb{P})}{P_{ij}} < c_1 < 1$. For $c_1 = c_2 = 1$, the lower bound and upper bound are equal and hence the optimal price will be the $j^{th}$ price in the price set $\mathbb{P}$. Therefore, $c_1$ and $c_2$ can be chosen to change the gap between the lower and upper bounds.
CHAPTER 4: PRICING MODEL EVALUATION

In the absence of optimal price values or the best hindsight strategy, it was important to the airline to define a set of offline and online metrics. Offline metrics are useful for model development, incremental learning, hyper-parameter optimization while online metrics measure business value. Establishing the exact set of offline metrics that correlates with online business metrics is an active area of research.

4.1 OFFLINE METRICS

In this section, we define the metrics that we use to serve as guides through hyper-parameter tuning and to ensure that nightly update of DNN weights do not overfit the data. We use the Price Decrease Recall (PDR) and Price Decrease Precision (PDP) scores presented by [31] due to their high correlation with the airline’s business metrics. PDR measures how likely our recommended prices are lower than the current offered prices for non purchased ancillary and PDP measures the percentage for recommended prices that are lower than current offered prices for non purchased ancillary. Additionally, we use the following metrics:

4.1.1 Area Under the Curve (AUC)

Due to presence of high class imbalance as discussed in Section 3.1, we used the AUC of the Receiver Operating Characteristic (ROC) Curve as the offline metric to compare ancillary purchase prediction model performance.

4.1.2 Regret Score (RS)

In recent work [31], regret score has been chosen as an offline evaluation criterion because of its proportional relationship to the business metric. RS is defined by equation (4.1).

\[
RS = \text{mean}_{\text{purchases}} \left( \max \left( 0, 1 - \frac{P_{\text{rec}}}{P} \right) \right)
\]  

(4.1)

Intuitively, RS measures on an average how close our recommended price \( P_{\text{rec}} \) was to the true purchase price \( P \). For the example set of sessions in Table 4.1, sessions 1, 2 and 5 have 0.20, 0.20 and 0.75 regret respectively. Because sessions 3 and 4 have recommended price higher than purchased, regret is 0. Therefore, \( RS \) values for this sample of sessions is 0.095.
Table 4.1: Example prices for purchased sessions

<table>
<thead>
<tr>
<th>Session #</th>
<th>Purchase Price</th>
<th>Recommended Price</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>10</td>
<td>8</td>
</tr>
<tr>
<td>2</td>
<td>15</td>
<td>12</td>
</tr>
<tr>
<td>3</td>
<td>10</td>
<td>15</td>
</tr>
<tr>
<td>4</td>
<td>25</td>
<td>35</td>
</tr>
<tr>
<td>5</td>
<td>40</td>
<td>37</td>
</tr>
</tbody>
</table>

4.1.3 Price Decrease F1 (PDF1)

This score is inspired by the F1 score used to evaluate the precision and recall trade-off. PDF1 therefore measures the trade-off between PDR and PDP according to (4.2).

\[ PDF1 = \frac{2 \cdot PDR \cdot PDP}{PDR + PDP} \]  \hspace{1cm} (4.2)

4.2 ONLINE METRICS

Online metrics represent real-world business metrics that indicate if a model is driving business value. We use two key metrics to measure the performance of a model in the real world.

4.2.1 Conversion Score

One of the primary business metric is the conversion ratio, i.e., the percentage of offers that are being purchased and converted into orders.

\[ \text{Conversion Score} = \frac{\text{Number of purchases}}{\text{Total number of sessions}} \]  \hspace{1cm} (4.3)

4.2.2 Revenue per session

The revenue per session (RPS) metric is one of the most essential business metrics to quantify actual performance.
4.3 TRAINING

All of our deep neural network models (in APP-DES and DNN-CL) are trained on NVIDIA Tesla K80 GPU. We used stochastic gradient descent (SGD)\cite{38} with a decaying learning rate to optimize the loss function. Mini-Batches and drop-out units \cite{39, 40} are used to regularize model training. For a discrete exhaustive search over the prices (see Section 3.2.2), we use a mini-batch of the allowed price inputs to enable a single call to the GPU which minimizes data transfer and model setup cost for each price selection event. Hyperparameters like $c_1$ and $c_2$ are tuned using the bounds for non-zero loss and the upper-lower bound gap (see Section 3.3) over the median price point in set $\mathbb{P}$. We also use the scheduled mini-batch training approach for online model training. Figure 4.1 shows online training loss values for incremental training of DNN based model.

![Figure 4.1: Loss curves for different online training sessions](image)

4.4 EXPERIMENTS

During the first phase of online experimentation, our airline partner’s business strategy is to recommend prices equal to or less than the current human-offered price. Although this strategy reduces the search space considerably, the business motivation behind it is to reduce the overall friction in the traveler’s journey by providing them an incentive to pre-purchase ancillaries online. Therefore, the aim of our online experiment is to offer discounts in an intelligent way, so that we improve the conversion rate of ancillaries without dropping the revenue per offer. This also has a potential negative impact of increasing conversion score without improving revenue per session. Therefore, as mentioned in Section 4, using the right set of metrics for evaluation is crucial.
4.4.1 Offline Experiments

We perform extensive offline experiments to evaluate the performance of the models before deployment. These offline experiments consist of two parts: (i) evaluating classifiers’ performance of ancillary purchase probability, and (ii) pricing effectiveness of a two-stage forecasting and optimization model versus a simultaneous, end-to-end pricing model.

Classifier Performance

It is critical to evaluate the performance of the ancillary purchase probability (APP) classifier since we are using it to estimate the demand function. Due to the high class imbalance present in the data, we used the AUC score to evaluate the performance. We started with Gaussian Naive Bayes with Clustering (GNBC) as our baseline to match the state of the art in the airline industry. We then ran the experiments with the Gaussian Naive Bayes (GNB), Random Forest (RF) and DNN classifiers, all of which performed better than the GNBC baseline. The AUC scores of 0.5716, 0.6273, 0.6633 and 0.7664 for GNBC, GNB, RF and DNN respectively, show that the DNN achieves a 33% improvement in the AUC score compared to our baseline. This improvement is intuitive because DNNs can capture more complex relationships between the input features to predict highly imbalanced classes.

![ROC curve for offline trained model](image)

Figure 4.2: ROC curve for offline trained model

To evaluate the learn-ability and robustness of the classifiers, three datasets with varying
amount of data are used. Datasets $A$, $B$ and $C$ have 41,000, 50,000 and 72,000 sessions respectively. Results from our experiments are in Table 4.2. DNN shows most dominant signs of learn-ability with increasing dataset size. The best performance of these classifiers on the validation set is also presented as an ROC curve in Figure 4.2.

<table>
<thead>
<tr>
<th>Dataset</th>
<th>GNBC</th>
<th>GNB</th>
<th>RF</th>
<th>DNN</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>0.5444</td>
<td>0.6013</td>
<td>0.6646</td>
<td>0.6755</td>
</tr>
<tr>
<td>B</td>
<td>0.5274</td>
<td>0.6186</td>
<td>0.6771</td>
<td>0.6967</td>
</tr>
<tr>
<td>C</td>
<td>0.5716</td>
<td>0.6273</td>
<td>0.6633</td>
<td>0.7664</td>
</tr>
</tbody>
</table>

Table 4.2: AUC score of models on datasets.

Pricing effectiveness of a sequential two-stage model versus a simultaneous end-to-end model

Although the DNN performs well for Ancillary Probability Prediction, it was important to also measure the effectiveness of the final price recommendations from each pricing model. We used the offline metrics defined in Section 4.1 to perform the comparison between the two-stage sequential forecasting and optimization models (APP-LM and APP-DES), and the simultaneous end-to-end pricing model (DNN-CL). Given the business requirement to provide discounts on the human-recommended price, we considered Regret Score (RS) and Price Decrease Recall (PDR) as more important than PDP and PDF1 [31]. Our results are summarized in Table 4.3. The APP-LM (which uses our baseline APP model and is manually tuned through a parameter search), serves as our baseline for pricing effectiveness. The inefficient performance of the APP-DES model on these metrics despite the estimation of a good APP model in the first step suggests that the price-demand relationship (see Figure 3.3) is not estimated accurately. This shortcoming is overcome by the end-to-end model (DNN-CL), which not only overcomes the effect of this inaccuracy but also outperforms the APP-LM on all four metrics.

<table>
<thead>
<tr>
<th>Scores</th>
<th>APP-LM</th>
<th>APP-DES</th>
<th>DNN-CL</th>
</tr>
</thead>
<tbody>
<tr>
<td>RS</td>
<td>0.0741</td>
<td>0.3776</td>
<td>0.0726</td>
</tr>
<tr>
<td>PDR</td>
<td>0.6366</td>
<td>0.6303</td>
<td>0.8294</td>
</tr>
<tr>
<td>PDP</td>
<td>0.9276</td>
<td>0.9320</td>
<td>0.9230</td>
</tr>
<tr>
<td>PDF1</td>
<td>0.7550</td>
<td>0.7520</td>
<td>0.8737</td>
</tr>
</tbody>
</table>
Hence, we conclude that the DNN-CL model not only minimizes the regret for not pricing high for purchased ancillaries, but also maximizes the likelihood of the recommended prices being low when ancillaries are not purchased.

4.4.2 Online Experiments

Our APP-LM model has been deployed in production on our partner airline’s internet booking engine for model validation. The APP-DES and the DNN-CL models are currently under deployment, following their successful performance according to the offline metrics.

Table 4.4: Conversion percentage and revenue generated by our model (APP-LM) compared to human-curated and random prices

<table>
<thead>
<tr>
<th>Pricing System</th>
<th>Avg. Revenue per Offer</th>
<th>Conversion Score</th>
</tr>
</thead>
<tbody>
<tr>
<td>HUMAN</td>
<td>1.00</td>
<td>10.18%</td>
</tr>
<tr>
<td>RANDOM</td>
<td>0.77</td>
<td>12.37%</td>
</tr>
<tr>
<td>APP-LM</td>
<td>1.10</td>
<td>13.92%</td>
</tr>
</tbody>
</table>

According to the airline’s business strategy, we introduced a random discount model in addition to the APP-LM model. This random discount model is allowed to recommend discounted prices based on Gaussian noise. There are two reasons for deploying a random price recommender. First, it establishes a baseline for conversion score improvements from discounted ancillaries. Second, it enables us to explore various prices and calibrate price sensitivity. The deployed models are compared with both human-curated static prices and prices from the random discount model. All three were deployed concurrently in an A/B testing setting for a period of 120 days. The results of this comparison for the most recent 30 days are shown in Table 4.4.

Figure 4.4 and Table 4.4 indicate that the random discount model is able to produce higher conversion rates than the human-curated pricing system. This not only demonstrates the existence of price sensitivity among customers, but also allows us to measure it. Additionally, the random discount model is unable to produce higher revenue per offer because it conflates the sub-markets’ demand and makes them indistinguishable, thus losing information.

Because customers’ price sensitivity is observed through the random discount model, a slight increase in the conversion score was expected in our deployed model APP-LM. The results in Table 4.4, Figure 4.3 and Figure 4.4 confirm this expectation. We observe a 36%

---

1The exact dates and revenue figures cannot be included due to proprietary, privacy and sensitivity restrictions
Figure 4.3: Revenue Per Offer by Each Pricing System Over Time

Figure 4.4: Conversion Score by Each Pricing System Over Time
increase in conversion rate, which is a 15% increase compared to the random discount model. More importantly, our model produces 10% more revenue than the human-curated pricing system. This implies that our model recommends lower prices to targeted customers such that the revenue per offer from our model can still outperform (or at least be comparable to) the human-curated pricing system. For revenue per offer and conversion score, we see that our model can indeed capture the market trend in a timely fashion. Furthermore, the clear trend of both higher revenue and higher conversion score with respect to the human-curated system indicate the accuracy of target discount with the customer’s context.
CHAPTER 5: META-LEARNING

As discussed in Chapter 4, the online business performance of our deployed models is, on average, consistently better than human rule-based approaches. However, as is apparent from Figure 5.1, no one model dominates in performance, resulting in an erratic trend in in the revenue per offer among the models deployed online. The results in Figure 5.1 are due to a pre-configured standard A/B testing framework in the system of a real airline, in which the percentage share of online traffic share for each model is given by Figure 5.2. The next question of interest, therefore, is a meta-learning approach that directs traffic efficiently to the right model for that session.

Figure 5.1: Model online performance on business metric

We now model the traffic share value as a meta-parameter, which can then be tuned for targeting traffic more effectively to the better performing model. Learning this parameter is therefore critical to identify the “winning” model and separate it from other models. Based on customers’ responses (to purchase an ancillary or not), we can reinforce the meta-parameters to adapt to the outcome. The multi-armed bandit approach is one such reinforcement learning technique that accomplishes this exact task.

5.1 MULTI-ARMED BANDIT APPROACH

The multi-armed bandit problem is an extensively studied reinforcement learning technique which is widely used as a part of A/B testing [41, 42]. Solving this problem involves
determining a sequence of decisions to choose from a given action space, with the reward associated with each action or ‘arm’ only partially known (or having a random component). The environment (‘nature’) reveals a reward after each action is taken, thereby also revealing more information about the random component of that action’s reward. The objective of the problem is to maximize the expected rewards, i.e., minimize the cumulative expected regret [43]. The bandit problem involves trade off between exploitation and exploration since the reward is only revealed for the chosen action. Hence, this problem setting makes it perfectly suitable for A/B testing. At each possible action step, the tradeoff made by the decision-maker is to exploit the action that has the highest expected tradeoff with the updated information available until that point, and to explore other actions to gather more information about the random component of the reward of those actions, to maximize gain in the long run.

In our framework, each of the multiple models is viewed as an arm of the multi-armed bandit problem. This enables the decision-maker to direct online traffic based on the customer’s response to the price offered by that arm. Hence, this meta-learning approach provides a trainable mechanism to allocate customer traffic to the arms during the test based on performance. Furthermore, meta-learning allows potentially different expected conversion rates of the different arms in an online setting. We explore one of the techniques to solve the multi-arm bandit problem, called Thompson Sampling , to allow us to exploit arms that have performed well in the past and explore seemingly inferior arms in case it might outperform the current winning arm [44, 45].

Figure 5.2: Online traffic share and discount points
5.2 THOMPSON SAMPLING FOR THE BERNOULLI BANDIT

In a Bernoulli bandit problem, there are a total of $A$ valid actions. An action $a_t \subseteq A$ at time $t$ produces a reward $r_t \in \{0, 1\}$ of one with probability $\theta_a$ and zero with probability $1 - \theta_a$. The mean reward $\theta = (\theta_1, \ldots, \theta_A)$ is assumed to be unknown, but is constant over time. The agent begins with an independent prior belief over each $\theta_k$. As observations are gathered, the distribution is updated according to Bayes rule. The priors, according to equation 5.1, are assumed to be beta-distributed with parameters $\alpha_a \in \{\alpha_1, \ldots, \alpha_A\}$ and $\beta_a \in \{\beta_1, \ldots, \beta_A\}$. In particular, the exact prior probability density function given for an action $a$ is,

$$p_{\text{beta}}(\theta_a) = \frac{\Gamma(\alpha_a + \beta_a)}{\Gamma(\alpha_a)\Gamma(\beta_a)} \theta_a^{(\alpha_a-1)}(1 - \theta_a)^{(\beta_a-1)}$$ (5.1)

where $\Gamma$ denotes the gamma function. The beta distribution is particularly suited to this computation because it is a conjugate prior to the Bernoulli distribution [45].

5.2.1 Simulation

In this section we discuss an offline simulation performed on synthetic data to show the convergence rate of Thompson Sampling. Here, we have initialized three experimental models that have a success rate of 0.45, 0.55 and 0.60. The aim of this simulation is to achieve this success rate through multi-armed bandit approach. The algorithm 3 presents the pseudocode of the implementation used for simulation.

**Algorithm 3** Thompson Sampling for the Bernoulli Bandit

1: for $t = 1, 2, \ldots$ do
2: for $a = 1, \ldots, A$ do
3: Sample $\hat{\theta}_a \sim \text{Beta}(\alpha_a, \beta_a)$
4: end for
5: $x_t \leftarrow \text{argmax}_a \hat{\theta}_a$
6: Apply $x_t$
7: Observe $r_t$
8: $(\alpha_{x_t}, \beta_{x_t}) \leftarrow (\alpha_{x_t} + r_t, \beta_{x_t} + 1 - r_t)$
9: end for

We start the simulation with the prior $\theta^0 = \text{Beta}(\alpha = 1, \beta = 1)$, which corresponds to a uniform prior between 0 and 1. Note the initial uniform distribution can be seen in Figure 5.3. The run is then simulated for 2000 steps and target probabilities are recorded. In practice, the simulation results converged in approximately 1000 steps. Table 5.1 shows
the convergence of the Thompson Sampling approach for the multi-armed bandit problem, demonstrating that the latent probability distribution can be inferred using this approach.

<table>
<thead>
<tr>
<th>$\theta$</th>
<th>True probability</th>
<th>Simulated probability</th>
<th>Trials</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\theta_1$</td>
<td>0.45</td>
<td>0.45</td>
<td>70</td>
</tr>
<tr>
<td>$\theta_2$</td>
<td>0.55</td>
<td>0.55</td>
<td>305</td>
</tr>
<tr>
<td>$\theta_3$</td>
<td>0.60</td>
<td>0.61</td>
<td>1625</td>
</tr>
</tbody>
</table>

The visualization of the convergence in the beta distribution with respect to the iterations is shown in Figure 5.3. We thus conclude that convergence in finding the best arm can be achieved in a controlled environment where the latent probability distribution is temporally invariant, i.e., it belongs to a stationary system. For problems involving temporal dependence, convergence can only be estimated in an online setting, i.e., instantaneous environment and agent response [46].

Figure 5.3: Convergence of the Distribution using Thompson Sampling
5.3 CONSTRAINTS, CONTEXT AND CAUTION

Thompson sampling can be applied fruitfully to a broad array of online decision problems beyond the Bernoulli bandit. Thompson sampling outperforms other stochastic bandit algorithms (KL-UCB, Bayes UCB, UCB, \(\epsilon\)-greedy etc) on most bandit-type problems [44]. But in problems involving time-varying constraints on the action, line 5 in Algorithm 3 has to be modified.

Another extension of the multi-armed bandit approach addresses contextual online decision problems. In these problems, the choice of the arm in a multi-armed bandit also depends on an independent random variable \(z_t\) that the agent observes prior to making the decision. In such scenarios, the conditional distribution of the response \(y_t\) is of the form \(p_\theta(\cdot|a_t, z_t)\). Contextual bandit problems of this kind can be addressed through augmenting the action space and introducing time-varying constraint sets by viewing action and constraint together as \(\tilde{a}_t = (a_t, z_t)\), with each arm (choice) represented as \(\tilde{A}_t = \{(a_t, z_t : a \in A)\}\), where \(A\) is the set from which \(x_t\) must be chosen. After which it is straightforward to apply thompson sampling to select action.

In certain situations when models have a particular baseline criteria to maintain, caution-based sampling can be used [45]. This can be accomplished through constraining actions for each time \(t^{th}\) step to have lower bound on expected average reward as \(A_t = \{a \in A : E[r_t|a_t = a] \geq \tilde{r}\}\). This ensures that expected average reward at least exceeds \(\tilde{r}\) using such actions.

5.4 NON-STATIONARY SYSTEMS AND CONCURRENCE

So far, we discussed settings in which model parameters \(\theta\) are constant over time i.e. belong to a stationary system. In practice, the decision-maker could face a non-stationary system, which is more appropriately modeled by time-varying parameters, such that reward is generated by \(p_\theta(\cdot|a_t)\). In such contexts, the arm of the problem will never stop exploring, which could be a potential drawback. A more robust method involves ignoring all historical observations made prior to a certain time period \(\tau\) in the past [47]. Now, decision-makers produce a posterior distribution after every time step \(t\) based on the prior and conditioned only on the most recent \(\tau\) actions and observations. Model parameters are sampled from this distribution, and an action is selected to optimize the associated model.

Dynamic pricing is one such problem where a single recommendation could be a weighted sum of recommendations from multiple arms, a concept referred to as concurrence [48]. This is a case where the decision-maker takes multiple actions (arms) concurrently. Concurrency
can be predefined with number of fixed arms to be pulled every time or it could be coupled with baseline caution (discussed in Section 5.3). This approach is similar to an approach based on an ensemble of models.

5.5 ONLINE IMPLEMENTATION FOR ANCILLARY PRICING AT DEEPAIR

Although the assumption of models being temporally stable is a crucial assumption while using Thompson Sampling in multi-armed bandit settings, the offline simulations we performed for meta-learning provide reasonable evidence of convergence to the true distribution [49, 50] of the choice of models. Hence, our meta-learning approach shows promising offline results on synthetic data. For online deployment in the airline’s systems, meta-learning using a multi-armed bandit approach can be used to route incoming customer bookings to each of the considered models, which serve as arms of the bandit. Additionally, meta-learning could also potentially handle concurrency by pricing using multiple models. Currently, meta-learning based models are being deployed to our partner airlines without concurrency being enabled, with the concurrency feature under development. Using targeted traffic routing, we hope to further improve our online metrics of evaluation as far as business value is considered. We are actively developing models that can improve the estimation accuracy.
CHAPTER 6: SUMMARY AND FUTURE WORK

6.1 DISCUSSION

Historically, price sensitivity to ancillaries has not been captured due to static pricing. However, it is critical to capture customers’ price sensitivity to price ancillaries correctly to match customer needs and maximize airline revenues. Currently, all of the models we proposed in Chapter 4 - APP-LM, APP-DES and DNN-CL - show promise, and are continually being tuned further to capture and train on the ground truth responses of customers. While APP-LM has been deployed online, APP-DES and DNN-CL are in the process of being deployed. Once model validation is performed online, the airline’s booking system will switch to the most robust model. For the APP-DES and DNN-CL models, we are specifically interested in further examining the correlation between offline model performance to online business performance, because they outperform APP-LM in offline experimentation. Further, our deployment system will be transitioned from a scheduled mini-batch training (see Section 4.3), to an event-wise online training. This transition will enable the model to accurately learn temporal dependencies. We also plan to alter the current business strategy (see Section 4.4) to allow our model to recommend prices higher than current limit, and observe customer responses. Finally, we plan to study the effect of heterogeneous ancillary types being dynamically priced by our deployed models, and the best predicted subset of ancillaries being offered to the customer. Given that various ancillaries compete for wallet-share and shelf-space, it will help expand our understanding of whether such pricing models compete, or collaborate, with each other.

6.2 CHALLENGES

In our study, we have shown that the estimation of the demand curve is possible by estimating the probability of purchase. The foundations of our pricing models like APP-LM and APP-DES are based on this (see Section 3.1) idea. Sequential estimation of demand curve including price optimization with high efficiency is a challenging task. This is due to the presence of variability in the estimation step, followed by sub-optimal solution of the price optimization problem. Challenges arise because the components of such sequential models can be highly interdependent and thereby susceptible to the co-variability. Practically, techniques like market wise clustering, ensembling of models and meta learning seems to be effective in mitigating the effects of high interdependence [51]. This is one of the reasons why
our cluster based models (GNBC) and ensemble of models (DNN) [39] are able to perform significantly better.

Also, we proposed our custom loss model as a better alternative to the current method of optimal pricing (see Section 3.3). We have also successfully demonstrated the significant improvement on overall performance of DNN-CL over APP based models as well as human rule-based approaches. However, a caveat corresponding to improved hyperparameter tuning needs to be addressed. Parameters that describe the lower and upper bounds of the loss function have to be tuned correctly in order to achieve superior performance of the DNN-CL model. Hence, the challenge is to find the optimal values for such hyperparameters without having any intuition behind the architecture. Additionally, hyperparameter search on two drastically different settings, namely online and offline, increases the complexity of the problem tremendously.

Finally, our meta-learning framework which aims to direct the traffic to specific models in an online setting is yet to be tested on real environment. Even though the offline simulation results in a controlled setting are promising, the customers ground truth response are yet to be measured. The temporal dependence on traffic routing probability can only be observed when meta-learning is performed live with customers making choices based on the models’ recommendations. Therefore, estimating the rate of convergence is another crucial challenge. Moreover, non-convergence of the probability distribution might lead to over-exploration. This challenge can only be addressed once the meta-learning receives feedback from the online environment.

6.3 CONCLUSION

In this work, we presented a first step in the direction of efficient customized pricing systems based on machine learning for ancillary prices from booking data in the airline industry, compared to past works that focus on strategic impacts. We successfully demonstrate that ancillaries can be dynamically priced without using any user specific information that violates customer privacy. We compared three different dynamic pricing models (APP-LM, APP-DES and DNN-CL) and their associated frameworks. Our results show that the accuracy of estimating the demand and fine-tuning its sensitivity to price, greatly influences the optimality of the recommended price. Our offline experiments indicate that DNN-CL can perform significantly better than APP-LM, APP-DES, and currently deployed approaches, to maximize revenue. In online experiments, our APP-LM model outperforms human-curated pricing systems currently in use. By using reliable evaluation metrics that correlate well with business impact, we hope to observe further improvement in online metrics through
our APP-DES and DNN-CL models that are currently under deployment. Furthermore, our work on meta-learning shows ancillary price recommendations from multiple concurrent models in a competitive setting. Our work demonstrates the promise of improved business value through highly accurately, continuously updated models for customer demand for ancillaries, and their sensitivity to prices.
REFERENCES


